

**Práctico N° 8 –Matemática 3°SH1/SE1**

1) a) Graficar la función  $f : f(x) = \begin{cases} x-1 \Leftrightarrow x < 0 \\ x+1 \Leftrightarrow x \geq 0 \end{cases}$

b) Calcular los límites que existan:

$$\lim_{x \rightarrow 0^+} f(x); \quad \lim_{x \rightarrow 0^-} f(x); \quad \lim_{x \rightarrow 0} f(x); \quad \lim_{x \rightarrow +\infty} f(x); \quad \lim_{x \rightarrow -\infty} f(x)$$

2) a) Graficar la función  $g : g(x) = \begin{cases} x^2 \Leftrightarrow x < 1 \\ x \Leftrightarrow 1 \leq x < 2 \\ 4-x \Leftrightarrow x \geq 2 \end{cases}$

b) Calcular los límites que existan:

$$\lim_{x \rightarrow 1^+} g(x); \quad \lim_{x \rightarrow 1^-} g(x); \quad \lim_{x \rightarrow 1} g(x); \quad \lim_{x \rightarrow +\infty} g(x); \quad \lim_{x \rightarrow -\infty} g(x); \quad \lim_{x \rightarrow 2^+} g(x); \quad \lim_{x \rightarrow 2^-} g(x); \quad \lim_{x \rightarrow 4} g(x)$$

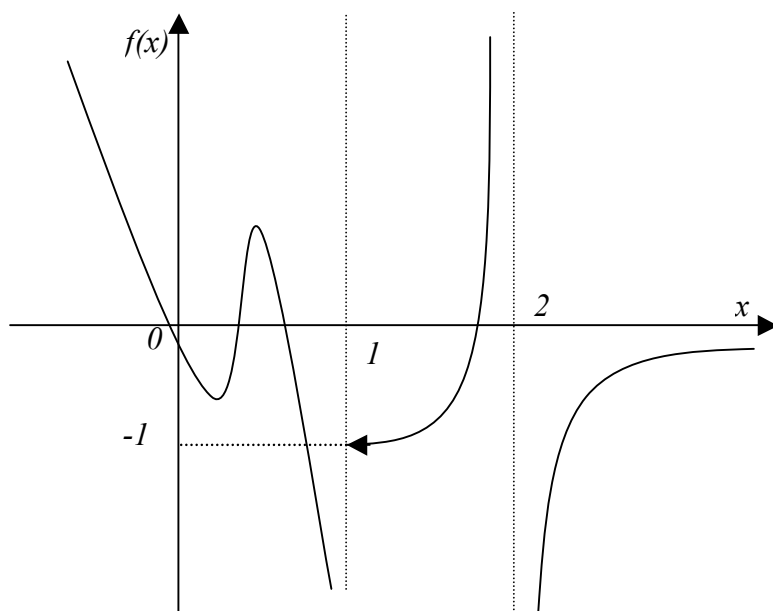
3) a) Graficar la función  $h : h(x) = \begin{cases} \frac{1}{x+2} \Leftrightarrow x \leq 1 \\ L|x-3| \Leftrightarrow x > 1 \end{cases}$

b) Hallar dominio de  $h$ .

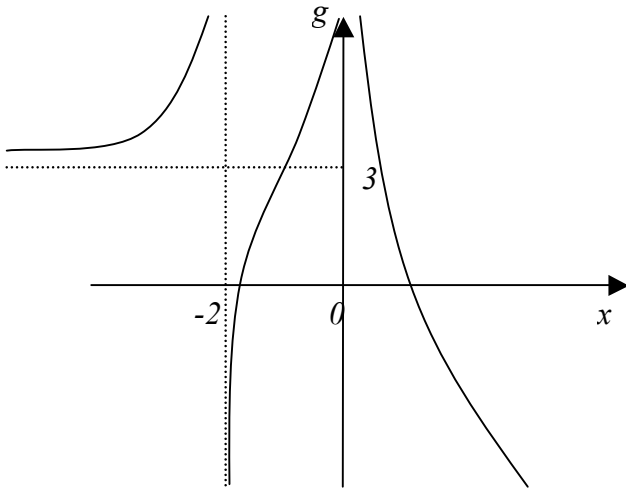
c) Calcular los límites que existan:

$$\lim_{x \rightarrow -\infty} h(x); \quad \lim_{x \rightarrow -2} h(x); \quad \lim_{x \rightarrow 1^-} h(x); \quad \lim_{x \rightarrow 1^+} h(x); \quad \lim_{x \rightarrow 3} h(x); \quad \lim_{x \rightarrow +\infty} h(x)$$

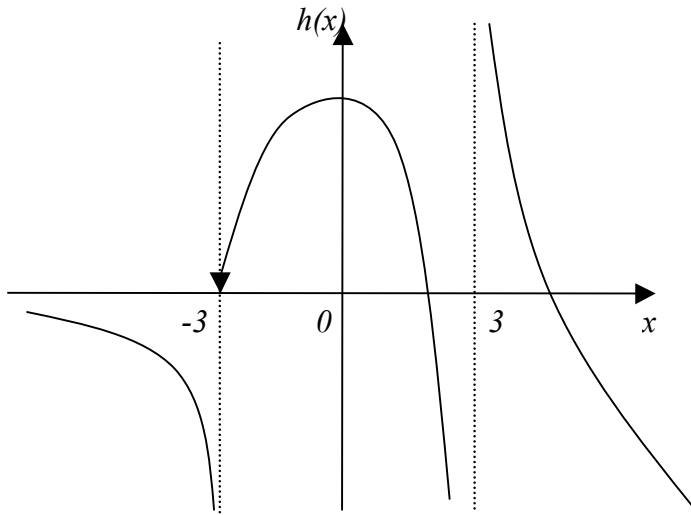
4) Indicar dominio de cada una de las funciones graficadas; y hallar los límites que se indican



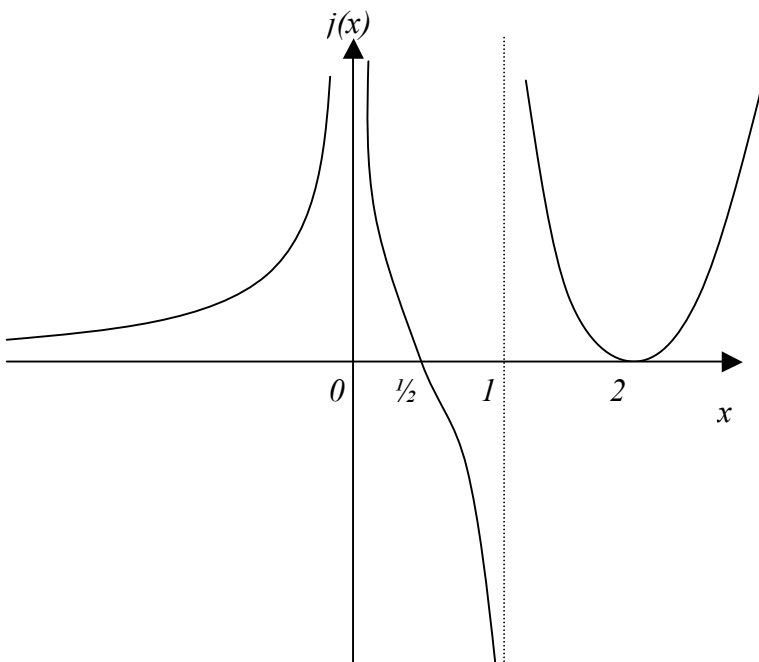
$$\begin{aligned} &\lim_{x \rightarrow 1^+} f(x) \\ &\lim_{x \rightarrow 1^-} f(x) \\ &\lim_{x \rightarrow 2^+} f(x) \\ &\lim_{x \rightarrow 2^-} f(x) \\ &\lim_{x \rightarrow +\infty} f(x) \\ &\lim_{x \rightarrow -\infty} f(x) \end{aligned}$$



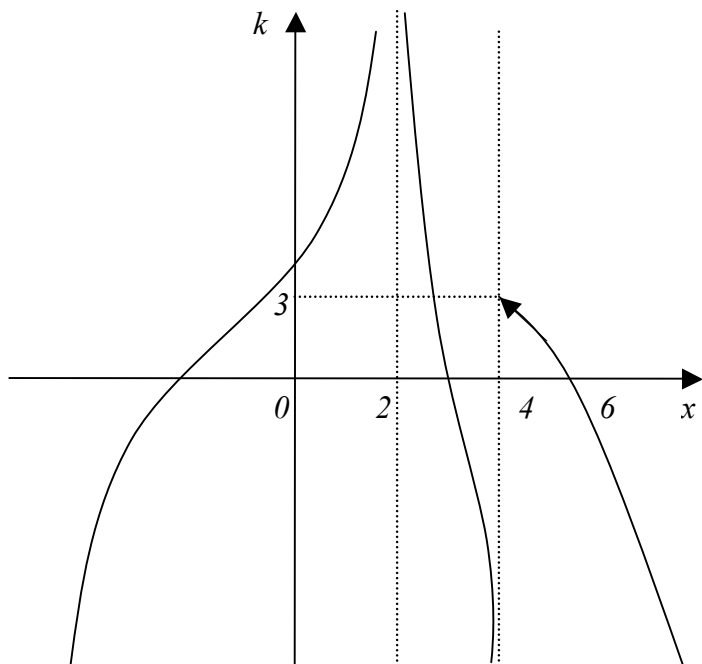
- $\lim_{x \rightarrow -2^-} g(x)$
- $\lim_{x \rightarrow -2^+} g(x)$
- $\lim_{x \rightarrow 0^-} g(x)$
- $\lim_{x \rightarrow 0^+} g(x)$
- $\lim_{x \rightarrow +\infty} g(x)$
- $\lim_{x \rightarrow -\infty} g(x)$



- $\lim_{x \rightarrow -3^-} h(x)$
- $\lim_{x \rightarrow -3^+} h(x)$
- $\lim_{x \rightarrow 3^-} h(x)$
- $\lim_{x \rightarrow 3^+} h(x)$
- $\lim_{x \rightarrow +\infty} h(x)$
- $\lim_{x \rightarrow -\infty} h(x)$



- $\lim_{x \rightarrow 0^+} j(x)$
- $\lim_{x \rightarrow 0^-} j(x)$
- $\lim_{x \rightarrow 1^+} j(x)$
- $\lim_{x \rightarrow 1^-} j(x)$
- $\lim_{x \rightarrow +\infty} j(x)$
- $\lim_{x \rightarrow -\infty} j(x)$



$$\lim_{x \rightarrow 2^+} k(x)$$

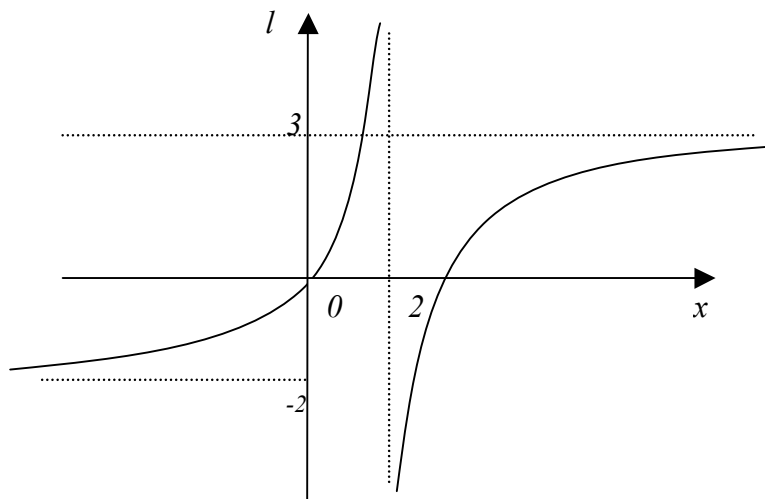
$$\lim_{x \rightarrow 2^-} k(x)$$

$$\lim_{x \rightarrow 4^+} k(x)$$

$$\lim_{x \rightarrow 4^-} k(x)$$

$$\lim_{x \rightarrow +\infty} k(x)$$

$$\lim_{x \rightarrow -\infty} k(x)$$

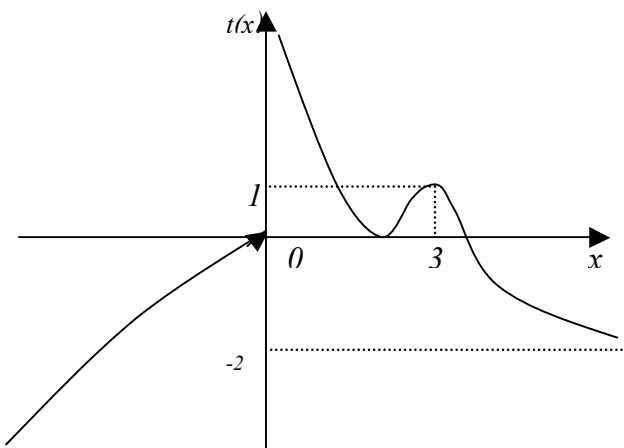


$$\lim_{x \rightarrow 2^+} l(x)$$

$$\lim_{x \rightarrow 2^-} l(x)$$

$$\lim_{x \rightarrow +\infty} l(x)$$

$$\lim_{x \rightarrow -\infty} l(x)$$



$$\lim_{x \rightarrow 0^+} t(x)$$

$$\lim_{x \rightarrow 0^-} t(x)$$

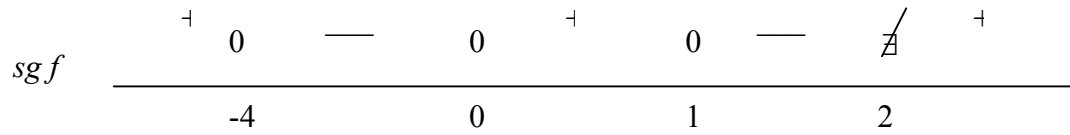
$$\lim_{x \rightarrow 3} t(x)$$

$$\lim_{x \rightarrow +\infty} t(x)$$

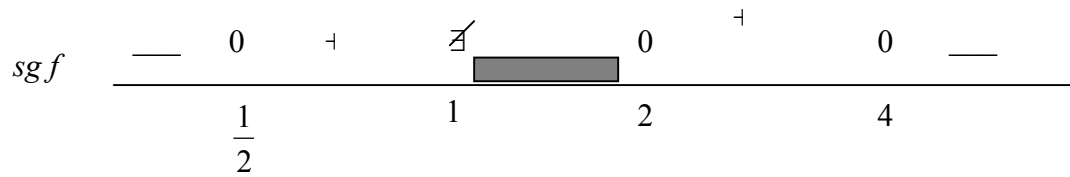
$$\lim_{x \rightarrow -\infty} t(x)$$

5) Representar en cada caso una función  $f$  que cumpla con los datos dados:

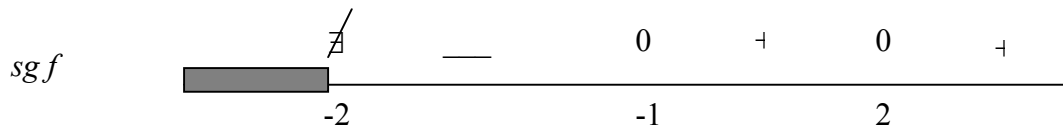
i)  $D(f) = \mathbb{R} - \{2\}$ ;  $\lim_{x \rightarrow 2^-} f(x) = -\infty$ ;  $\lim_{x \rightarrow +\infty} f(x) = 0$ ;  $\lim_{x \rightarrow -\infty} f(x) = +\infty$ ;  $\lim_{x \rightarrow 2^+} f(x) = +\infty$



ii)  $D(f) = (-\infty, 1) \cup [2, +\infty)$ ;  $\lim_{x \rightarrow 1^-} f(x) = +\infty$ ;  $\lim_{x \rightarrow +\infty} f(x) = -\infty$ ;  $\lim_{x \rightarrow -\infty} f(x) = -2$ ;  $f(0) = -\frac{1}{2}$

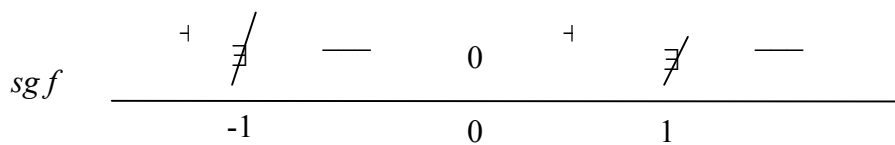


iii)  $D(f) = (-2, +\infty)$ ;  $\lim_{x \rightarrow -2^+} f(x) = -\infty$ ;  $\lim_{x \rightarrow +\infty} f(x) = +\infty$ ; ;  $f(0) = 1$



iv)  $D(f) = \mathbb{R} - \{-1, 1\}$   $\lim_{x \rightarrow 1^-} f(x) = +\infty$ ;  $\lim_{x \rightarrow 1^+} f(x) = -\infty$ ;  $\lim_{x \rightarrow -1^-} f(x) = 1$ ;

$\lim_{x \rightarrow +\infty} f(x) = -2$ ;  $\lim_{x \rightarrow -\infty} f(x) = +\infty$ ;  $\lim_{x \rightarrow 1^+} f(x) = -\infty$



v)  $D(f) = \mathbb{R} - \{0, 2\}$   $\lim_{x \rightarrow 2^+} f(x) = -\infty$ ;  $\lim_{x \rightarrow 2^-} f(x) = +\infty$ ;  $\lim_{x \rightarrow 0^+} f(x) = +\infty$ ;

$\lim_{x \rightarrow 0^-} f(x) = 0$ ;  $\lim_{x \rightarrow +\infty} f(x) = 0$ ;  $\lim_{x \rightarrow -\infty} f(x) = +\infty$ ;

